



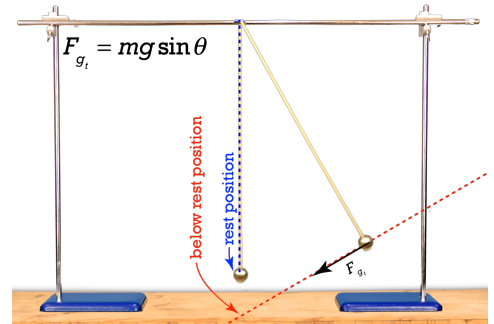
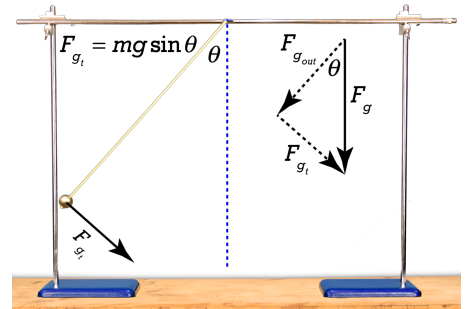
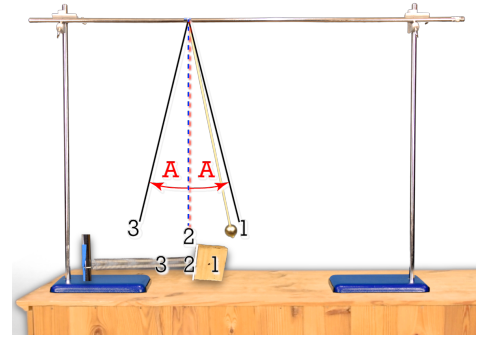
Flipping Physics Lecture Notes:

When is a Pendulum in Simple Harmonic Motion?

Mass-spring systems and pendulums are both in simple harmonic motion. Both oscillate around an equilibrium position and have a restoring force pointed towards the equilibrium position that increases proportionally with displacement from the equilibrium or rest position.

- The displacement from equilibrium position for a pendulum is an *angular* displacement.
 - Units are in degrees or radians.
 - Symbol is theta, θ .
 - Maximum displacement from equilibrium position is still Amplitude, A.
- The restoring force for a pendulum is the force of gravity tangential to the path of the pendulum. This force is:
 - Proportional to displacement from equilibrium position and
 - Directed toward equilibrium position.

Actually, the force of gravity tangential is only considered to be directed toward equilibrium or rest position for “small angles”. Typically I consider this to be less than 15° , however, some sources require the angle to be less than 10° . It depends on how much error you are willing to allow. The larger the angle, the larger the error. This is because of the *small angle approximation*.



Simple Harmonic Motion if $\theta < 15^\circ$

14°

This IS Simple Harmonic Motion

small angle approximation:
 $\sin \theta \approx \theta$ when $\theta < 15^\circ$

$\theta = 15^\circ \times \frac{\pi \text{ rad}}{180^\circ} = 0.2618 \text{ rad}$

$\sin(0.2618) = 0.2588 \approx 0.2618$