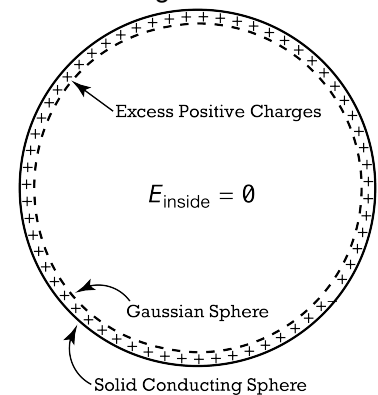


Conductors are materials where the electrons are free to move rather easily, however, when they are in electrostatic¹ equilibrium, this means the charges are stationary in the object. There are four things you need to remember about conductors in electrostatic equilibrium. These are the first three:

- 1) The electric field inside a conductor in electrostatic equilibrium equals zero. $E_{\text{inside}} = 0$
 - a. If the electric field inside were not equal to zero, charges would have a net electrostatic force acting on them and they would accelerate, therefore the conductor would not be in electrostatic equilibrium.
 - i. $E_{\text{inside}} \neq 0 \Rightarrow F_e = qE \neq 0 \Rightarrow$ not in electrostatic equilibrium
 - b. Notice that this means that anything inside a conductor in electrostatic equilibrium is shielded from all external electric fields. This is called electrostatic shielding.

- 2) All excess charges are located on the surface (or surfaces) of the conductor.
 - a. Solid conducting sphere example:
 - i. Draw a Gaussian surface as a concentric sphere with a radius slightly smaller than the radius of the sphere.
 - ii. Using Gauss' law, because there is no electric field inside the conductor in electrostatic equilibrium, we know the left-hand side of the equation equals zero.
 - iii. Therefore, there must be zero net charge inside the Gaussian sphere and all the excess charges must be outside the Gaussian sphere.
 - iv. Therefore, all the excess charges are on the surface of the conductor.



$$\Phi_E = \oint \vec{E} \cdot d\vec{A} = \frac{q_{\text{enclosed}}}{\epsilon_0} \quad \& \quad E_{\text{inside}} = 0 \Rightarrow 0 = \frac{q_{\text{enclosed}}}{\epsilon_0} \Rightarrow q_{\text{enclosed}} = 0$$

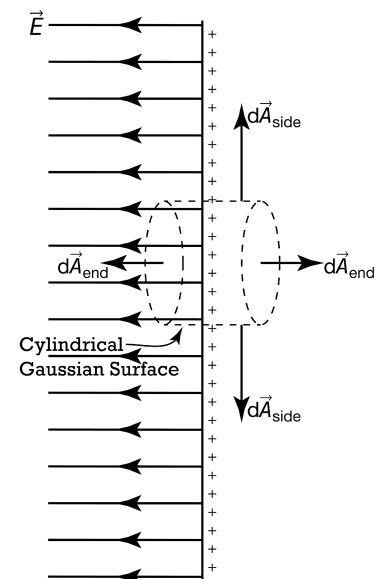
- 3) The electric field just outside the surface of a conductor in electrostatic equilibrium is:

$$E_{\text{just outside}} = \frac{\sigma_{\text{local}}}{\epsilon_0} \quad \& \quad \perp \text{ to surface}$$

- a. If the electric field had a component parallel to the surface of the conductor, the charges would move, and the conductor would no longer be in electrostatic equilibrium. Therefore, the electric field at the surface of a conductor in electrostatic equilibrium must be perpendicular to the surface.
 - i. Because equipotential surfaces are always perpendicular to the electric field, the surface of a conductor in electrostatic equilibrium must be an equipotential surface.

$$\Delta V = V_B - V_A = - \int_A^B \vec{E} \cdot d\vec{r} = - \int_A^B E \cos \theta dr = - \int_A^B E \cos(90^\circ) dr = 0$$

- b. If we zoom way in on the surface of the conductor in electrostatic equilibrium, we can draw a Gaussian cylinder with its cylindrical axis normal to the surface of the conductor.



¹ Electrostatics is the study of electromagnetic phenomena that occur when there are no moving charges.

$$\Phi_E = \oint \vec{E} \cdot d\vec{A} = \frac{q_{\text{enclosed}}}{\epsilon_0}$$

$$\Rightarrow \Phi_E = \int_{\text{side}} E dA \cos \theta_{\text{side}} + \int_{\text{left end}} E dA \cos \theta_{\text{end}} + \int_{\text{right end}} E dA \cos \theta_{\text{end}} = \frac{q_{\text{enclosed}}}{\epsilon_0}$$

$$\Rightarrow \int_{\text{side}} E dA \cos(90^\circ) + \int_{\text{left end}} E dA \cos(0^\circ) + \int_{\text{right end}} (0) dA \cos \theta_{\text{end}} = \frac{q_{\text{enclosed}}}{\epsilon_0}$$

$$\& \sigma = \frac{Q}{A} \Rightarrow \sigma_{\text{local}} = \frac{q_{\text{in}}}{A_{\text{end}}} \Rightarrow q_{\text{in}} = \sigma_{\text{local}} A_{\text{end}}$$

$$\Rightarrow E \int_{\text{left end}} dA = E A_{\text{end}} = \frac{\sigma_{\text{local}} A_{\text{end}}}{\epsilon_0} \Rightarrow E = \frac{\sigma_{\text{local}}}{\epsilon_0}$$

The fourth thing you need to remember about conductors in electrostatic equilibrium is in my video:

- "Irregularly Shaped Conductors in Electrostatic Equilibrium"
- <http://www.flippingphysics.com/electrostatic-equilibrium-irregular-shape.html>