

Introduction to Faraday's Law of Induction
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AP Physics C – Video Lecture Notes
Chapter 31-32
Thank You, Emily Rencsok, for these notes.

- Moving charges cause a B field
- Moving poles cause an E field
- If B field changes/time, charge flows + induced current + induced emf
- Faraday's Law of Induction

$$\mathcal{E} = -N \frac{d\Phi_B}{dt}$$

↑ induced emf ↑ # of loops

$$\Phi_B = BA \cos \theta \quad \mathcal{E} = -N \frac{d}{dt} (BA \cos \theta)$$

Can induce emf by changing:

- 1) magnitude of B field
- 2) area enclosed by loop
- 3) θ btwn \vec{A} + \vec{B}
- 4) Any combination of other 3

Introduction to Lenz' Law - The Direction of Faraday's Law of Induction (with Examples)

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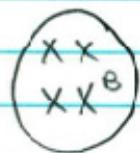
- Direction of induced current

Lenz' Law

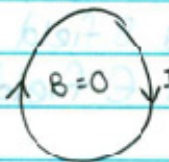
$$\mathcal{E} = -N \frac{d\Phi_B}{dt}$$

induced emf is opposite the change in Φ_B
(electromagnetic inertia)

$B_{in} +$ increasing
 $B_{ind} \Rightarrow$ out
 $I_{ind} \Rightarrow$ counterclockwise



i



f

$B_{in} +$ decreasing
 $B_{ind} \Rightarrow$ into board
 $I_{ind} \Rightarrow$ clockwise



i



f

$B_{in} \Phi_B$ decreasing
 $B_{ind} \Rightarrow$ into board
 $I_{ind} \Rightarrow$ clockwise



i



f

$B_{out} +$ increasing
 $B_{ind} \Rightarrow$ into board
 $I_{ind} \Rightarrow$ CW



i



f

(i) $\Phi_B = 0$
 (f) Φ_B inc + out of board
 $B_{ind} \Rightarrow$ into board
 $I_{ind} \Rightarrow$ CW



i



f

(i) $\Phi_B = 0$
 (f) Φ_B inc + into board
 $B_{ind} \Rightarrow$ out
 $I_{ind} \Rightarrow$ CCW

Derivation of Motional EMF using Net Force

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The diagram shows a rod of length l moving to the right with velocity v in a magnetic field B directed into the page (indicated by 'X' marks). The magnetic force $F_B = qvB$ acts on the charges in the rod. An induced electric field E is shown pointing downwards, with an electric force $F_e = qE$ acting on the charges. The forces are balanced, resulting in zero net force on the charges.

Equations derived:

$$\sum F_y = F_B - F_e = ma_y = 0$$

$$qvB \sin \theta = qE$$

$$vB \sin 90^\circ = E$$

$$vB = E$$

$$\Delta V = Ed$$

$$\Delta V = vBl$$

$$E = vBl \quad \text{motional emf}$$

Derivation of Motional EMF using Faraday's Law of Induction

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$\mathcal{E} = -N \frac{d\Phi_B}{dt}$

Φ_B into board + increasing
 $B_{ind} \Rightarrow$ out of board
 $I_{ind} \Rightarrow$ CCW

$\Phi_B = BA \cos \theta$

$\mathcal{E} = -N \frac{d\Phi_B}{dt}$

$\mathcal{E} = -(1) \frac{d}{dt} (BA \cos \theta)$
 $= -B \cos(180) \frac{d}{dt} (lx)$
 $= Bl \frac{dx}{dt} = Blv$

Faraday's Law of Induction Example - Changing Current on a Resistance Loop

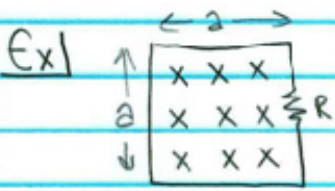
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Ex 1



$\mathcal{E} = -N \frac{d\Phi_B}{dt}$
 $= -(1) \frac{d}{dt} (BA \cos \theta)$
 $\mathcal{E} = -a^2 \cos \theta \frac{d}{dt} (45 \cos(17t))$
 $\mathcal{E} = -a^2 765 \sin(17t)$
 $\Delta V = IR$
 $I = \frac{\Delta V}{R}$
 $I = \frac{1}{R} (765 a^2 \sin(17t))$
 $I = \frac{1}{25} (765 (0.05)^2 \sin(17t))$
 $I = 0.0765 \sin(17t)$
 $I(t) = 76.5 \sin(17t) \text{ mA}$
 $A = 76.5 \text{ mA}$
 $\omega = 17 = \frac{\Delta \theta}{\Delta t} = \frac{2\pi}{T} = 2\pi f$
 $f = \frac{\omega}{2\pi} = \frac{17}{2\pi} = 2.71 \text{ Hz}$

$R = 25.0 \Omega$
 $a = 5.00 \text{ cm}$
 $B = (45.0 \cos(17t)) \text{ T}$
 $I(t) = \text{mag?}$
 $f = ?$

Example - Rotating Metal Bar in Constant Magnetic Field (Motional EMF)

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Ex) $v = r\omega$ $\Delta V = vBl$

$\Delta V = ?$

$$\int d\mathcal{E} = \int Bv dr$$

$$\mathcal{E} = \int Bv dr$$

$$\mathcal{E} = B \int v dr$$

$$\mathcal{E} = B \int r\omega dr$$

$$\mathcal{E} = B\omega \int_0^l r dr$$

$$\mathcal{E} = B\omega \left[\frac{1}{2}r^2 \right]_0^l$$

$$\boxed{\mathcal{E} = \frac{B\omega l^2}{2}}$$

Introduction to Generators and Motors

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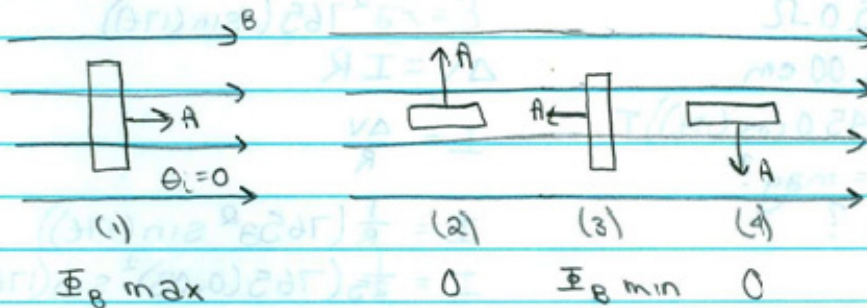
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- Generators + motors

ME → EE EE → ME
 CE → ME

Generator



$$\Phi_B = BA \cos \theta$$

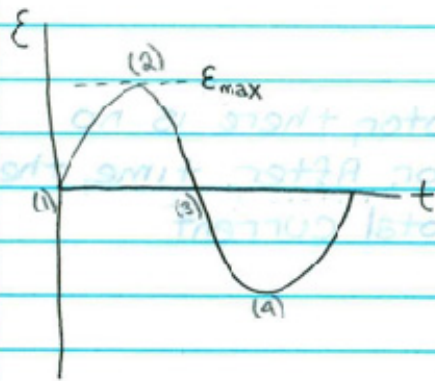
$$\omega = \frac{\Delta \theta}{\Delta t} = \frac{\theta}{t} \rightarrow \theta = \omega t$$

set $\theta_i = 0$ + $t_i = 0$

$$\Phi_B = BA \cos(\omega t)$$

$$\mathcal{E} = -N \frac{d\Phi_B}{dt} = -N \frac{d}{dt} (BA \cos(\omega t)) = -NBA \frac{d}{dt} \cos(\omega t)$$

$$\mathcal{E} = -NBA(-\sin \omega t)\omega \rightarrow \mathcal{E} = \omega NBA \sin(\omega t) \quad \boxed{\mathcal{E}_{\text{max}} = \omega NBA}$$



for a generator

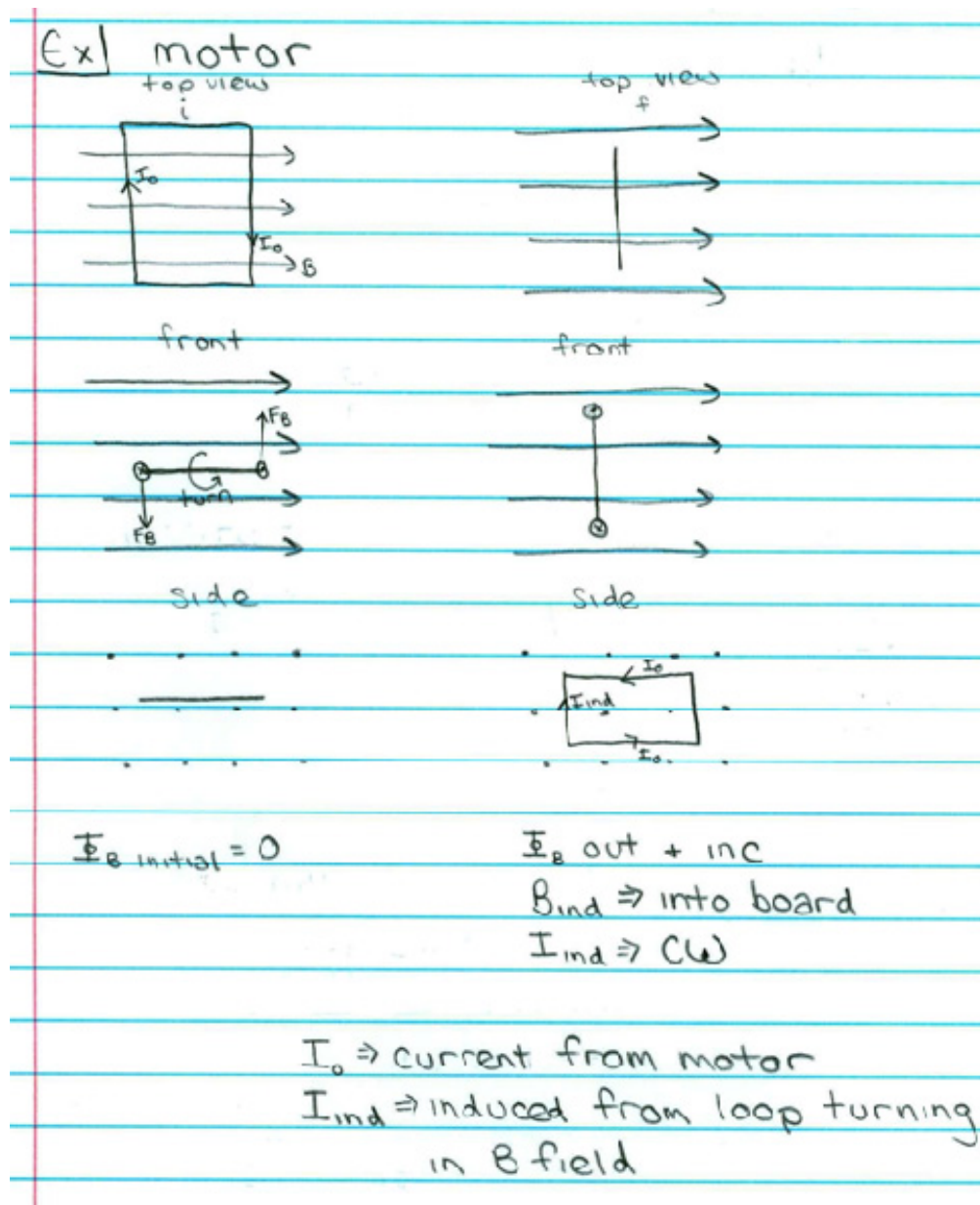
Derivation of Back EMF in an Electric Motor

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- Back emf

- When you start up a motor, there is no induced emf in the motor. After time, the back emf reduces the total current

Example - Back EMF in an Electric Motor

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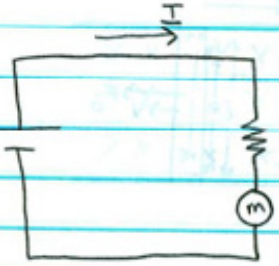
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(#9 was the Eddy Current Demo and there weren't any lecture notes to go along with that one, in case you were looking for them.)

Ex) motor 120V circuit
 $R_m = 5.00 \Omega$
 @ Full speed, $I = 2.40 \text{ A}$



a) $\mathcal{E}_{\text{back}} = ?$
 b) I @ start
 c) $\frac{P_{\text{start}}}{P_{\text{run}}}$

@ full speed

a) $\Delta V_{\text{loop}} = 0 = -\Delta V_R - \mathcal{E}_{\text{back}} + \Delta V_{\mathcal{E}}$
 $0 = -IR - \mathcal{E}_{\text{back}} + \Delta V_{\mathcal{E}}$
 $\mathcal{E}_{\text{back}} = \Delta V_{\mathcal{E}} - IR$
 $\mathcal{E}_{\text{back}} = 120 - 2.4(5)$
 $\mathcal{E}_{\text{back}} = 108 \text{ V}$

@ beginning, no $\mathcal{E}_{\text{back}}$

b) $\Delta V_{\text{loop}} = 0 = -\Delta V_R + \Delta V_{\mathcal{E}}$
 $\Delta V_{\mathcal{E}} = IR$
 $120 = I(5)$ $I_{\text{start}} = 24 \text{ A}$

c) $\frac{(I_{\text{start}})^2 R}{(I_{\text{run}})^2 R} = \frac{24^2}{2.4^2} = 100$

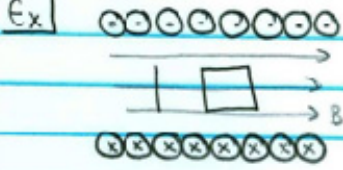
Example - Current Carrying Square Loop in a Solenoid

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Ex | 

$\mathcal{E} = -N_L \frac{d\Phi_B}{dt}$ $\Phi_B = BA \cos \theta$

$\mathcal{E} = -N_L \frac{d}{dt} (\mu_0 n I d^2 \cos \omega t)$ $B = \mu_0 n I$

$\mathcal{E} = -N_L \mu_0 n I d^2 \frac{d}{dt} (\cos \omega t)$ $A = d^2$

$\omega = \frac{d\theta}{dt} = \frac{\theta_f - \theta_i}{t_f - t_i} = \frac{\theta}{t}$

$\mathcal{E} = N_L \mu_0 n I d^2 \omega \sin(\omega t)$ $\theta = \omega t$

$\mathcal{E} = 150(4\pi \times 10^{-7})(500)(20)(0.02)^2(2\pi) \sin(2\pi t)$

$\mathcal{E} = 0.004732 \sin(2\pi t)$

Square loop in solenoid

- Turn by mechanical means

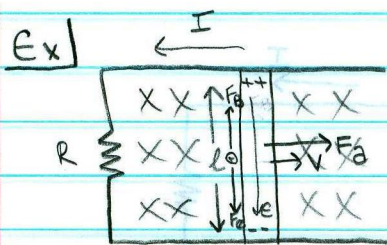
$N_L = 150$ $\mathcal{E}(t) = ?$

$d_{\text{side}} = 0.020 \text{ m}$

$\omega = 2\pi \text{ rad/s}$

$\mathcal{E} = 0.00473 \sin(2\pi t) \text{ V}$

Example - Power and Motional EMF
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$$\sum F_y = F_B - F_e = ma_y = 0$$

$$F_B = F_e$$

$$vB \sin \theta = \mathcal{E}$$

$$\mathcal{E} = vB$$

$$\Delta V = -\mathcal{E}d$$

$$|\Delta V| = \mathcal{E}d$$

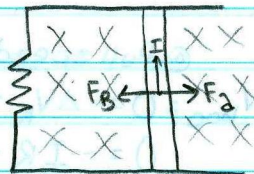
$$\Delta V = vBl$$

$$B = 1.5 \text{ T}$$

$$v = 5.0 \text{ m/s}$$

$$R = 2.0 \ \Omega$$

$$l = 25 \text{ cm}$$



$$\sum F_x = F_a - F_B = ma_x = 0$$

$$F_a = F_B$$

$$F_a = I l B \sin \theta$$

$$= I l B \sin 90$$

$$F_a = \frac{vBl}{R} l B$$

$$F_a = \frac{vB^2 l^2}{R} = \boxed{0.35 \text{ N}}$$

a) $F_a = ?$

b) $P_{F_a} = ?$

c) $P_R = ?$

$$\Delta V = IR$$

$$I = \frac{\Delta V}{R} = \frac{vBl}{R}$$

b) $P_{F_a} = F_a v \cos \theta$

$$= \frac{vB^2 l^2}{R} v \cos 0 = \boxed{1.8 \text{ W}}$$

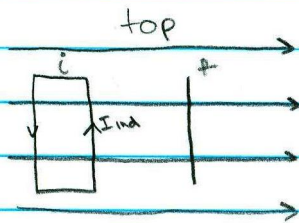
c) $P_e = I \Delta V$

$$P_e = \left(\frac{vBl}{R} \right) (vBl)$$

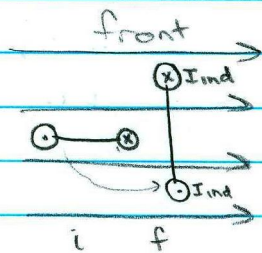
$$P_R = \frac{v^2 B^2 l^2}{R}$$

$$\boxed{P_R = 1.8 \text{ W}}$$

- Generator



$$\frac{d\Phi_B}{dt}$$



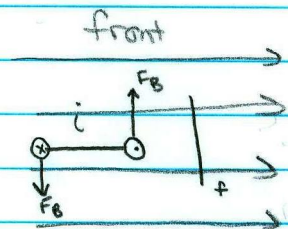
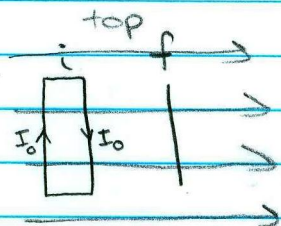
$$\Phi_B = 0 \text{ i}$$

$$\Phi_B \text{ right } f \text{ + inc}$$

$$B_{ind} \Rightarrow \text{left}$$

$$I_{ind} \Rightarrow$$

- Motor



Torque in same direction
as we turned it

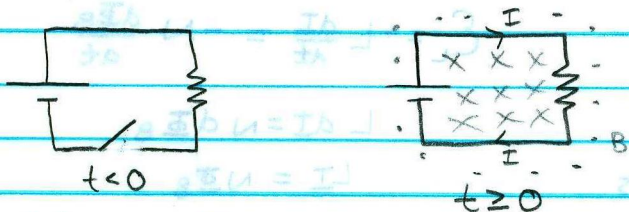
Derivation of Inductance of a Coil and Self Inductance of a Solenoid

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$$\Phi_{B_i} = 0$$

$$\Phi_{B_f} = \text{into board} + \text{inc}$$

$$B_{\text{ind}} = \text{out}$$

$$I_{\text{ind}} = \text{CCW}$$

Self-inductance

$$\mathcal{E}_{\text{ind}} = -N \frac{d\Phi_B}{dt}$$

$$\Phi_B = BA \cos \theta$$

$$B = \frac{\mu_0 I}{2\pi r}$$

$$\mathcal{E}_{\text{ind}} \propto \frac{dI}{dt}$$

$$\mathcal{E}_L = -L \frac{dI}{dt}$$

L is the inductance of the coil

$$\int \mathcal{E}_L \frac{dI}{dt} = \int N \frac{d\Phi_B}{dt}$$

$$L dI = N d\Phi_B$$

$$LI = N \Phi_B$$

$$L = \frac{N \Phi_B}{I}$$

not on eqn sheet

$$L = - \frac{\mathcal{E}_L}{dI/dt}$$

$$L \Rightarrow \frac{V}{A/s} = \frac{V \cdot s}{A} = \text{Henry, H}$$

$$R = \frac{\Delta V}{I} \rightarrow \text{resistance to current}$$

$$L = - \frac{\mathcal{E}_L}{dI/dt} \rightarrow \text{resistance to a change in current}$$

Example - Inductance and Induced EMF on a Solenoid

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Ex) Solenoid

$$\frac{dI}{dt} = 75.0 \text{ A/s}$$

$$N = 500.0 \text{ turns}$$

$$l = 50.0 \text{ cm}$$

$$r = 4.0 \text{ cm}$$

$$\mathcal{E}_L = -L \frac{dI}{dt} = -N \frac{d\Phi_B}{dt}$$

$$L dI = N d\Phi_B$$

$$LI = N \Phi_B$$

$$L = \frac{N \Phi_B}{I} = \frac{N B A \cos \theta}{I}$$

a) $L = ?$

b) $\mathcal{E}_{ind} = ?$

$$L = \frac{N B A \cos \theta}{I}$$

$$L = \frac{N A}{l} \left(\mu_0 \frac{N}{l} I \right)$$

$$L = \frac{\mu_0 A N^2}{l}$$

$$L = \frac{(4\pi \times 10^{-7}) (\pi (0.04)^2) (500)^2}{0.5}$$

$$L = 0.003158$$

$$L = 3.16 \text{ mH}$$

$$\mathcal{E}_{ind} = -L \frac{dI}{dt}$$

$$\mathcal{E}_{ind} = -(0.003158)(75)$$

$$\mathcal{E}_{ind} = -237 \text{ mV}$$

Derivation of Current as Function of Time in an RL Circuit (Putting Energy into the Inductor)

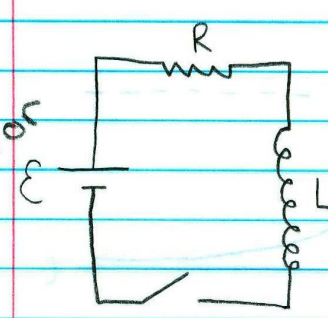
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Energy into inductor



RL Circuit

$$\Delta V_{\text{loop}} = 0 = \mathcal{E} - \Delta V_R - \Delta V_L$$

$$0 = \mathcal{E} - IR - L \frac{dI}{dt}$$

$$0 = \frac{\mathcal{E}}{R} - I - \frac{L}{R} \frac{dI}{dt} \quad \text{let } x = \frac{\mathcal{E}}{R} - I$$

$$dx = -dI$$

$t < 0$
Close switch
at $t = 0$

Limits
@ $t = 0$ $[I_i = 0 \quad \frac{dI}{dt} \text{ max}]$

$$0 = \mathcal{E} - L \frac{dI}{dt}$$

$$L \frac{dI}{dt} = \mathcal{E}$$

$$\frac{dI}{dt} = \frac{\mathcal{E}}{L} \text{ (max)}$$

@ $t = \infty$
 $[\frac{dI}{dt} = 0 \quad I_f \text{ max}]$

$$0 = \mathcal{E} - IR$$

$$IR = \mathcal{E}$$

$$I = \frac{\mathcal{E}}{R} \text{ (max)}$$

$$\Delta V_{\text{loop}} = 0 = \mathcal{E} - \Delta V_R - \Delta V_L$$

$$0 = \mathcal{E} - IR - L \frac{dI}{dt}$$

$$0 = \frac{\mathcal{E}}{R} - I - \frac{L}{R} \frac{dI}{dt}$$

$$\text{let } x = \frac{\mathcal{E}}{R} - I$$

$$dx = -dI$$

$$0 = x - \frac{L}{R} \frac{dx}{dt}$$

$$0 = x + \frac{L}{R} \frac{dx}{dt}$$

$$-\frac{L}{R} \frac{dx}{dt} = x$$

$$\int \frac{dx}{x} = \int \frac{-R dt}{L}$$

$$\int_{x_i}^{x_f} \frac{1}{x} dx = - \int_0^t \frac{R}{L} dt$$

$$[\ln x]_{x_i}^{x_f} = \left[-\frac{R}{L} t \right]_0^t$$

$$\ln x_f - \ln x_i = -\frac{R}{L} t$$

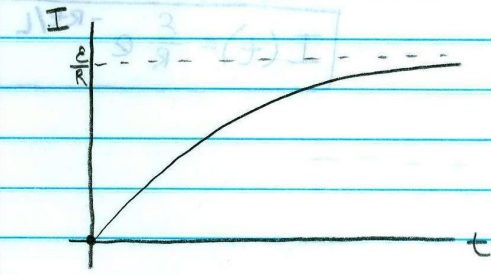
$$e^{\ln \frac{x_f}{x_i}} = e^{-\frac{R}{L} t}$$

$$\frac{x_f}{x_i} = e^{-Rt/L}$$

$$x_f = x_i e^{-Rt/L}$$

$$\frac{\mathcal{E}}{R} - I_f = \left(\frac{\mathcal{E}}{R} - I_i \right) e^{-Rt/L}$$

$$-I_f = \frac{\mathcal{E}}{R} e^{-Rt/L} - \frac{\mathcal{E}}{R}$$

$$I_f = \frac{\mathcal{E}}{R} (1 - e^{-Rt/L})$$


$$\tau = \frac{L}{R}$$

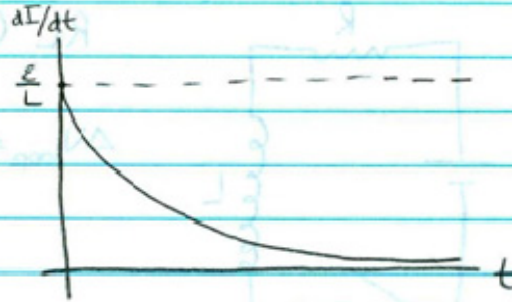
$$I(t) = \frac{\mathcal{E}}{R} (1 - e^{-t/\tau})$$

63.2% change

$$I = \frac{\mathcal{E}}{R} - \frac{\mathcal{E}}{R} e^{-Rt/L}$$

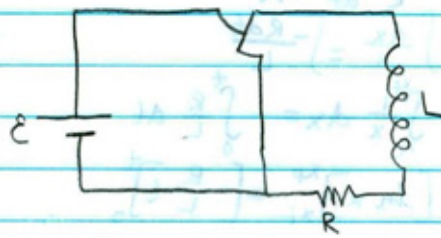
$$\frac{dI}{dt} = \frac{\mathcal{E}}{R} \frac{R}{L} e^{-Rt/L}$$

$$\frac{dI}{dt}(t) = \frac{\mathcal{E}}{L} e^{-Rt/L}$$



Derivation of Current as Function of Time in an RL Circuit (Removing Energy from the Inductor) - 17
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Energy
out of
inductor



Remove battery

$$\Delta V_{\text{loop}} = 0 = \mathcal{E} - \Delta V_R - \Delta V_L$$

$$0 = \mathcal{E} - IR - L \frac{dI}{dt}$$

$$IR = -L \frac{dI}{dt}$$

$$-\frac{R}{L} dt = \frac{dI}{I}$$

$$-\int_0^t \frac{R}{L} dt = \int_{I_i}^{I_f} \frac{dI}{I}$$

$$\left[-\frac{Rt}{L}\right]_0^t = \left[\ln I\right]_{I_i}^{I_f}$$

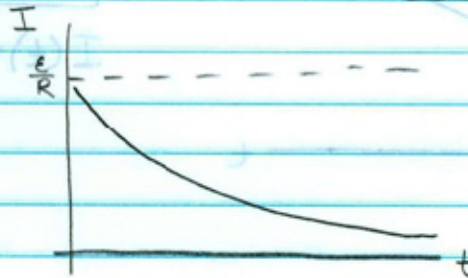
$$-\frac{Rt}{L} = \ln I_f - \ln I_i$$

$$e^{-\frac{Rt}{L}} = \frac{I_f}{I_i}$$

$$\frac{I_f}{I_i} = e^{-Rt/L}$$

$$I_f = I_i e^{-Rt/L}$$

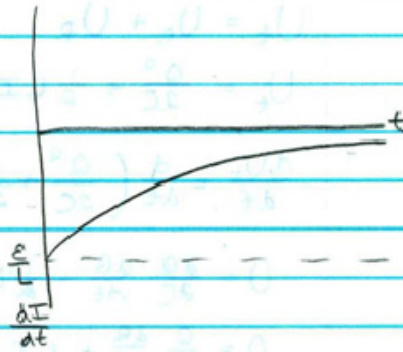
$$I(t) = \frac{\mathcal{E}}{R} e^{-Rt/L}$$



$$\frac{dI}{dt} = \frac{d}{dt} \left[\frac{\mathcal{E}}{R} e^{-Rt/L} \right]$$

$$\frac{dI}{dt} = \frac{\mathcal{E}}{R} \left(-\frac{R}{L} \right) e^{-Rt/L}$$

$$\boxed{\frac{dI}{dt}(t) = -\frac{\mathcal{E}}{L} e^{-Rt/L}}$$



Derivation of Energy stored in the Magnetic Field of an Inductor

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$$\Delta V = 0 = \mathcal{E} - IR - L \frac{dI}{dt}$$
$$\mathcal{E} = IR + L \frac{dI}{dt}$$
$$P = I\mathcal{E} = I^2 R + LI \frac{dI}{dt}$$

Power delivered by battery (points to $I\mathcal{E}$)
power dissipated by resistor (points to $I^2 R$)
power stored in B field of inductor (points to $LI \frac{dI}{dt}$)

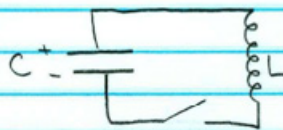
$$P = \frac{dU}{dt} = LI \frac{dI}{dt}$$
$$\int dU = \int LI dI$$
$$U = \int_0^I LI dI$$
$$U_L = \left[\frac{LI^2}{2} \right]_0^I$$
$$U_L = \frac{1}{2} LI^2$$

energy stored in the B field of an inductor (points to $U_L = \frac{1}{2} LI^2$)

The Last New AP Physics C - Derivation of Simple Harmonic Motion of an LC Circuit - 19
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- The last new subject

LC circuit



$t < 0$

close switch

@ $t = 0$

$$U_t = U_c + U_f$$

$$U_t = \frac{Q^2}{2C} + \frac{1}{2}LI^2$$

$Q + I$ change

$I_{\max} \rightarrow Q = 0$

$$\frac{dU_t}{dt} = \frac{d}{dt} \left(\frac{Q^2}{2C} + \frac{1}{2}LI^2 \right) = 0 \quad Q_{\max} \rightarrow I = 0$$

$$0 = \frac{2Q}{2C} \frac{dQ}{dt} + \frac{1}{2}L(2I) \frac{dI}{dt}$$

$$0 = \frac{Q}{C} \frac{dQ}{dt} + LI \frac{dI}{dt}$$

$$I = \frac{dQ}{dt}$$

$$0 = \frac{Q}{C} I + LI \frac{d^2Q}{dt^2}$$

$$\frac{dI}{dt} = \frac{d^2Q}{dt^2}$$

$$0 = \frac{Q}{C} + L \frac{d^2Q}{dt^2}$$

$$-\frac{Q}{C} = L \frac{d^2Q}{dt^2}$$

$$\boxed{\frac{d^2Q}{dt^2} = -\frac{1}{LC} Q}$$

$$\frac{d^2x}{dt^2} = -\omega^2 x$$

$$\omega = \sqrt{\frac{1}{LC}} = \frac{1}{\sqrt{LC}}$$

$$Q(t) = Q_{\max} \cos\left(\frac{1}{\sqrt{LC}}t + \theta\right) \quad x(t) = A \cos(\omega t + \theta)$$

@ $t = 0$, $Q_i = Q_{\max}$, so $\theta = 0^\circ$

$$\boxed{Q(t) = Q_{\max} \cos\left(\frac{1}{\sqrt{LC}}t\right)}$$

$$I = \frac{dQ}{dt} = \frac{d}{dt} \left(Q_{\max} \cos\left(\frac{1}{\sqrt{LC}}t\right) \right)$$

$$\boxed{I(t) = -\frac{Q_{\max}}{\sqrt{LC}} \sin\left(\frac{t}{\sqrt{LC}}\right)}$$

Example - Current and Potential Difference in an RL Circuit

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AP Physics C - Video Lecture Notes

Chapter 31-32

Thank You, Emily Rencsok, for these notes.

Ex) RL circuit

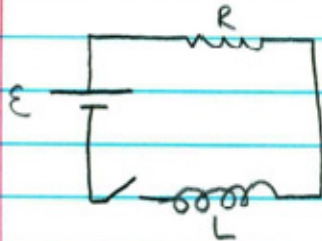
$$L = 4.5 \text{ H}$$

$$a) \Delta V_L = ? @ I = 1.50 \text{ A}$$

$$R = 6.0 \ \Omega$$

$$b) I_{\text{max}} = ?$$

$$\mathcal{E} = 24 \text{ V}$$



$$\Delta V_{\text{loop}} = 0 = \mathcal{E} - \Delta V_R - \Delta V_L$$

$$\Delta V_L = \mathcal{E} - \Delta V_R = \mathcal{E} - IR$$

$$\Delta V_L = 24 - 1.5(6) = \boxed{15 \text{ V}}$$

$I_{\text{max}} @ t \approx \infty$

when $\frac{dI}{dt} = 0$

$$0 = \mathcal{E} - \Delta V_R - \Delta V_L$$

$$\Delta V_L = 0$$

$$0 = \mathcal{E} - IR$$

$$IR = \mathcal{E}$$

$$I = \frac{\mathcal{E}}{R} = \frac{24}{6} = \boxed{4.0 \text{ A}}$$

Example - A Battery, Resistor, Capacitor and Inductor in a Circuit

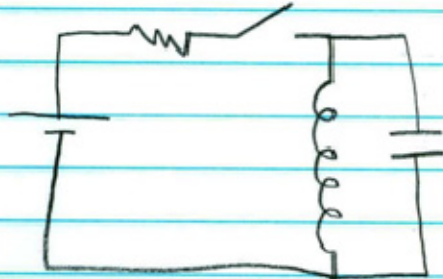
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Thank You, Emily Rencsok, for these notes.

Ex



$$\mathcal{E} = 12 \text{ V}$$

$$R = 4.0 \, \Omega$$

$$L = 2.0 \text{ H}$$

$$C = 0.020 \text{ F}$$

$$a) U_{L(\max)} = ?$$

$$b) Q_{(\max)} = ?$$

closed for long time, opened
at $t = 0$

$$Q_i = 0$$

$$U_L = \frac{1}{2} L I^2$$

$$\text{max } I_{\max} = ? = I_i$$

$$\Delta V = IR$$

$$U_{L \max} = \frac{1}{2} (2)(3)^2$$

$$I_L = \frac{\mathcal{E}}{R} = \frac{12}{4} = 3.0 \text{ A}$$

$$U_{L \max} = 9.0 \text{ J}$$

$$Q_{\max} = ?$$

$$U_{L \max} = U_{C \max}$$

$$9 = U_{C \max} = \frac{Q_{\max}^2}{2C}$$

$$\sqrt{2(9)(0.02)} = Q_{\max}$$

$$Q_{\max} = 0.60 \text{ C}$$

- $\mathcal{E} = -N \frac{d\Phi_B}{dt}$

$\mathcal{E} = -N \frac{d}{dt} (BA \cos \theta)$

RHR = *change in flux (Lenz' Law)

- Motional emf

$\Delta V = vBl$

- derive

- memorize

↑ assumes θ btwn $v + B$ is 90°

$F_B = qvB \sin \theta$

- Generators

$\mathcal{E}(t) = \omega NBA \sin(\omega t)$

$\omega = \frac{\Delta \theta}{\Delta t} = \frac{\theta}{t}$ $\theta_{t=0} = 0$
 $\theta = \omega t$

- derive

- memorize

- Back emf = 0 when motor isn't spinning

- $L = \frac{N\Phi_B}{I}$ - derive

- memorize

- RL Circuit

$I(t) = \frac{\mathcal{E}}{R} (1 - e^{-t/\tau})$ $\tau = \frac{L}{R}$ (derive + know limits)

$U_L = \frac{1}{2} LI^2$

- LC circuit \rightarrow SHM (memorize + derive)

$\omega = \frac{1}{\sqrt{LC}} = \frac{\Delta \theta}{\Delta t} = \frac{2\pi}{T}$