



Flipping Physics Lecture Notes:
Electric Flux

<http://www.flippingphysics.com/electric-flux.html>

Flux is defined as any effect that appears to pass or travel through a surface or substance, however, realize that effect does not need to move. Hence, "appears to".

Electric flux is the measure of the amount of electric field which passes through a defined area. The equation for electric flux of a uniform electric field is:

- $\Phi_E = \vec{E} \cdot \vec{A} = EA \cos \theta$

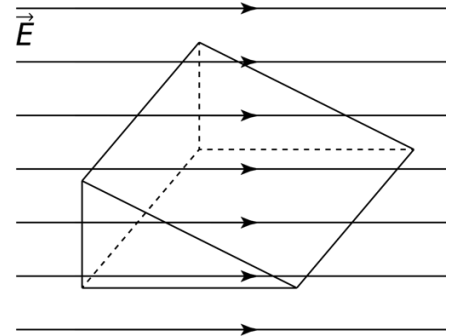
- Φ is the uppercase, Greek letter phi
- E is the uniform electric field (*use magnitude*)
- A is the area of the surface through which the uniform electric field is passing (*use magnitude*)
- θ is the angle between the directions of E and A
 - Notice this is the same form as the equation for work. This means you use the magnitudes of E and A, and $\cos \theta$ determines if the electric flux is positive or negative

- $W = \vec{F} \cdot \Delta \vec{r} = F \Delta r \cos \theta$

- Electric flux is a scalar

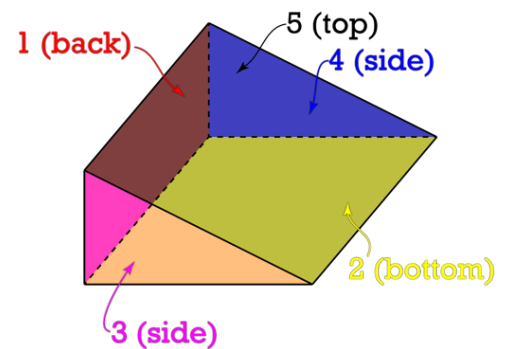
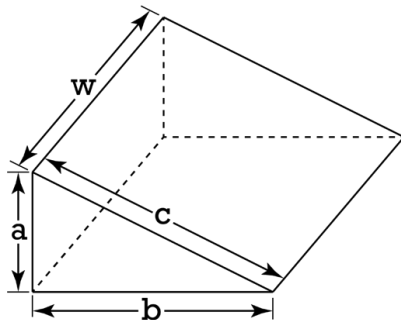
$$\frac{N \cdot m^2}{C}$$

- The units for electric flux are $\frac{N \cdot m^2}{C}$

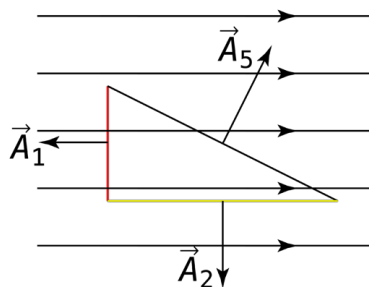


Usually, electric flux is through some sort of closed surface. So, let's do an example and determine the net electric flux of a uniform, horizontal electric field through a right triangular box.

Let's define and label the dimensions and sides of the triangular box as:



And now we can determine the electric flux through each side:



Electric flux for Area 1 (back): θ_1 is 180° because Area 1 is to the left or out of the rectangular box and the electric field is to the right.

$$\Phi_1 = EA_1 \cos \theta_1 = E (aw) \cos (180^\circ) = -Eaw$$

Electric flux for Area 2 (bottom): θ_2 is 90° because Area 2 is down or out of the rectangular box and the electric field is to the right.

$$\Phi_2 = EA_2 \cos \theta_2 = E (bw) \cos (90^\circ) = 0$$

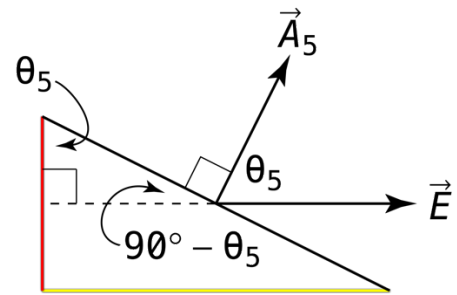
Electric flux for Areas 3 and 4 (sides): θ_3 and θ_4 are both 90° because Area 3 is out of the page and Area 4 is into the page (and the electric field is to the right).

$$\Phi_3 = EA_3 \cos\theta_3 = E\left(\frac{1}{2}ba\right) \cos(90^\circ) = 0 = \Phi_4$$

Electric flux for Area 5 (top): To understand why $\cos\theta_5 = a/c$, we need to draw another diagram.

$$\cos\theta_5 = \frac{A}{H} = \frac{a}{c}$$

$$\Phi_5 = EA_5 \cos\theta_5 = E(cw) \left(\frac{a}{c}\right) = Eaw$$



And the total electric flux through the entire triangular box is:

$$\Phi_{\text{total}} = \Phi_1 + \Phi_2 + \Phi_3 + \Phi_4 + \Phi_5 = -Eaw + 0 + 0 + 0 + Eaw = 0$$

Notice that:

- When an electric field is going into a closed surface, the electric flux is negative.
- When an electric field is coming out of a closed surface, the electric flux is positive.