

$$I \equiv \frac{dq}{dt}$$

Electric current, I , is defined as the derivative of charge with respect to time:

- $I \equiv \frac{dq}{dt} \Rightarrow \frac{\text{coulombs, } C}{\text{seconds, } s} = \text{amperes, } A$
 - Amperes are a base S.I. unit.
 - This is instantaneous current.

$$I_{\text{average}} = \frac{\Delta Q}{\Delta t}$$

- Current is the electric charge of the charges which pass by a point in a current carrying wire divided by the time it takes for those charges to pass by that point.
- Current occurs when there is an electric potential difference across a wire. If there is no electric potential difference, current does not flow.

$$\Delta V = 0 \Rightarrow I = 0$$

Unless otherwise stated, electric current in this class is all considered to be *conventional current*:

- The direction of conventional current is the direction positive charges *would* flow.
- Reality is that, in most circuits, negative charge carries (electrons, e^-) move opposite the direction of conventional current.

Let's look at charges flowing in a wire:

Start with the average current over a small section of the wire Δx :

$$I_{\text{average}} = \frac{\Delta Q}{\Delta t}$$

$$\Delta Q = (\# \text{ of charge carriers}) (\text{charge per carrier, } q)$$

• Charge carrier density, n :

$$n = \frac{\# \text{ of charge carriers}}{\text{volume, } V} \Rightarrow \# \text{ of charge carriers} = nV$$

$$\Rightarrow \Delta Q = nVq \ \& \ V = A\Delta x \Rightarrow \Delta Q = nA\Delta xq$$

$$V_{\text{drift}} = v_d = \frac{\Delta x}{\Delta t} \Rightarrow \Delta x = v_d \Delta t$$

- Drift velocity, v_d : The average velocity of the charge carriers in a current carrying wire.
 - If the current is zero, the charge carriers are still moving, however, the average velocity of the charge carriers is zero.
 - v_d typically is quite low. On the order of 0.1 mm/s. The reason lightbulbs in a circuit (for example) turn on immediately when you flip the switch is because all the electrons are already in the wire. When you flip the switch, they all start flowing.

$$\Rightarrow \Delta Q = nAv_d \Delta t q \Rightarrow I = \frac{\Delta Q}{\Delta t} = \frac{nAv_d \Delta t q}{\Delta t} \Rightarrow I = nAv_d q$$

