

Flipping Physics Lecture Notes: Ampère's Law Review for AP Physics C: Electricity and Magnetism <u>http://www.flippingphysics.com/ampere.html</u>

Ampère's law is the magnetic field equivalent to Gauss' law:

$$\Phi_{E} = \oint \vec{E} \cdot d\vec{A} = \frac{q_{\text{in}}}{\varepsilon_{0}}$$

- Gauss' law:
 - Closed surface integral and charge inside a Gaussian surface.

$$\oint \vec{B} \cdot d\vec{s} = \mu_0 I_{\text{in}}$$

- Ampère's law:
 - Closed loop integral and current inside an Amperian loop.

Example: Determine the magnitude of the magnetic field outside an infinitely long, straight, wire with radius R and current I.

Start by drawing an Amperian loop in the shape of a circuit of radius $r \ge R$ which is concentric with the wire. And let's use Ampère's law.



$$\Rightarrow \oint B ds \cos \theta = \oint B ds \cos \theta^{\circ} = B \oint ds = B (2\pi r) = \mu_{\theta} I_{\text{in}}$$
$$\Rightarrow B = \frac{\mu_{\theta} I}{2\pi r}$$