

Torque = τ (VECTOR!)

2 types of motion:

translational: caused by force

rotational: caused by torque

* mass is a measure of inertia (the ability to resist a change in motion)

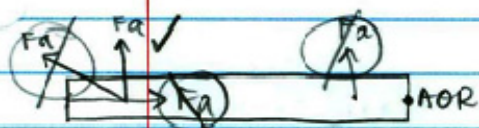
torque is the ability of a force to cause an angular acceleration (α).

$$\tau = f d \sin \theta$$

F = force

d = lever arm; distance from the force to the axis of rotation

θ = angle between the force & lever arm



$$\sin \theta = 90^\circ$$

dimensions = $N \cdot m = \text{Joule}$

Video Lecture #2 – Introduction to the Right Hand Rule for Torque

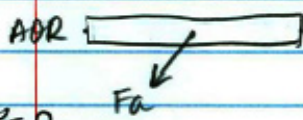
Right hand rule



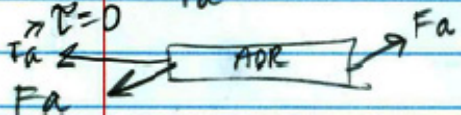
- τ (into the board)



+ τ (out of the board)



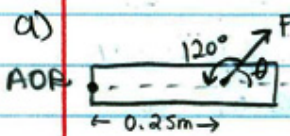
- τ (into the board)



+ τ (out of the board)

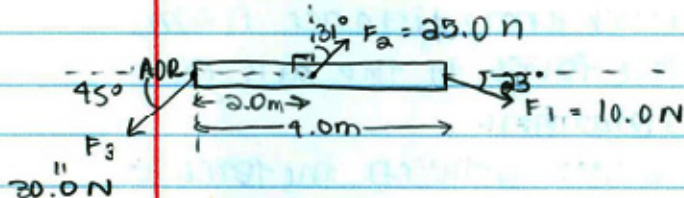
+ τ (out of the board)

0.282 #1 | $\tau = ??$ $F_a = 3.0\text{ N}$ $\theta = 60.0^\circ$ $d = 0.25\text{ m}$
 $\tau_{\text{max}} = ??$

a)  $\tau = Fd \sin \theta$
 $= (3)(0.25)(\sin 120)$
 $= 0.6495190508$
 $\tau \approx 0.65 \text{ N}\cdot\text{m}$

b) $\tau_{\text{max}} = Fd \sin \theta$
 $= (3)(0.25)(\sin 90)$
 $\tau_{\text{max}} \approx 0.75 \text{ N}\cdot\text{m}$

0.282 #3 | $\tau_{\text{net}} = ??$



$\tau_3 = F_1 d_1 \sin \theta_1 \Rightarrow (10.0)(4.0)(\sin 25) = -15.3696 \text{ N}\cdot\text{m}$

$\tau_2 = F_2 d_2 \sin \theta_2 \Rightarrow (25.0)(2.0)(\sin 90) = +42.85836504 \text{ N}\cdot\text{m}$

$\tau_1 = F_3 d_3 \sin \theta_3 \Rightarrow (30.0)(0)(\sin \theta_1) = 0 \text{ N}\cdot\text{m}$

$\tau_{\text{net}} = \tau_1 + \tau_2 + \tau_3$
 $= (-15.3696) + (42.85836504) + 0$
 $= 27.229$

$\tau_{\text{net}} \approx 27 \text{ N}\cdot\text{m}$

equilibrium

translational

$\sum \vec{F} = 0 = m\vec{a}$

$a = 0 \frac{\text{m}}{\text{s}^2}$ therefore the object is at rest or moving at a constant velocity

rotational

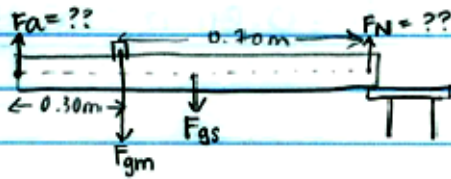
$\sum \vec{\tau} = 0 = I\alpha$ AOR

$\alpha = 0 \frac{\text{rad}}{\text{s}^2}$ therefore the object is at rest or @ constant angular velocity

static: both translational & rotational
 you can pick any AOR

Video Lecture #6 – In Introductory Rotational Equilibrium Problem

ex) $m_m = 0.50 \text{ kg}$ $m_{\text{stick}} = 88.6 \text{ g} \approx 0.0886 \text{ kg}$



$$\sum F_y = +F_a - F_{gm} - F_{gs} + F_N = m a_y = 0$$

$$\sum \tau = \tau_{F_a} - \tau_{F_{gm}} - \tau_{F_{gs}} + \tau_{F_N} = 0$$

$$\text{AOR @ } F_a = F_{gm} d_m \sin \theta_m - F_{gs} d_s \sin \theta_s + F_N d_N \sin \theta_N = 0$$

$$-m g d_m \sin \theta_m - m_{\text{stick}} g d_s \sin \theta_s + F_N d_N \sin \theta_N = 0$$

$$-(0.50)(9.8)(0.30)(\sin 90) - (0.0886)(9.8)(0.5) \sin 90 + F_N(1) \sin 90 = 0$$

$$-1.47 - 0.43414 + F_N(1) \sin 90 = 0$$

$$F_N = 1.90414$$

$$\boxed{F_N \approx 1.9 \text{ N}}$$

$$\sum \tau = -\tau_{F_a} - \tau_{F_{gm}} + \tau_{F_{gs}} + \tau_{F_N} = 0$$

$$\text{AOR @ } F_N = -F_a d_a \sin \theta_a + F_{gm} d_m \sin \theta_m - F_{gs} d_s \sin \theta_s = 0$$

$$-F_a d_a \sin \theta_a + m g d_m \sin \theta_m - m_{\text{stick}} g d_s \sin \theta_s = 0$$

$$-F_a(1) \sin 90 + (0.50)(9.8)(0.70) \sin 90 - (0.0886)(9.8)(0.5) \sin 90 = 0$$

$$F_a = 3.86414$$

$$\boxed{F_a \approx 3.9 \text{ N}}$$

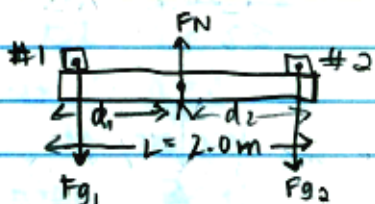
Video Lecture #7 – Page 288 #2a Finding the Fulcrum Location for Static Equilibrium on a Seesaw

D.288 #2a) $F_{g1} = 400 \text{ N}$

$L = 2.0 \text{ m}$

$F_{g2} = 300 \text{ N}$

$m_{\text{seesaw}} = 0 \text{ kg}$



$$\sum \tau = +\tau_{F_{g1}} - \tau_{F_N} - \tau_{F_{g2}} = 0$$

$$F_{g1} d_1 \sin \theta_1 - F_{g2} d_2 \sin \theta_2 = 0$$

$$(400)(d_1) \sin 90 - (300)(d_2) \sin 90 = 0$$

$$400 d_1 - 300 d_2 = 0$$

$$400 d_1 - 300(2 - d_1) = 0$$

$$400 d_1 - 600 + 300 d_1 = 0$$

$$700 d_1 = 600$$

$$d_1 = 0.8571428571$$

$$\boxed{d_1 \approx 0.86 \text{ m from } 400 \text{ m child}}$$